# Structure Determination of $\zeta_{2}-\mathbf{M n}_{\mathbf{5}} \mathbf{G e}_{\mathbf{2}}$ Using a Mixed Crystal 

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#### Abstract

$M_{r}=419 \cdot 87$, trigonal, $P 3 c 1, \quad a=7 \cdot 198(1), \quad c=$ $13 \cdot 076$ (1) $\AA, V=586 \cdot 7 \AA^{3}, Z=6(30 \mathrm{Mn}$ and 12 Ge per unit cell), $D_{x}=7 \cdot 129 \mathrm{Mg} \mathrm{m}^{-3}, \quad \lambda($ Mo $K \alpha)=$ $0 \cdot 71069 \AA, \quad \mu=31 \cdot 0 \mathrm{~mm}^{-1}, \quad F(000)=1134 \cdot 0, \quad T=$ 295 K . The crystal structure of $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$ has been determined using diffraction data derived from a mixed crystal of $\zeta_{1}-\mathrm{Mn}_{5 \cdot 11} \mathrm{Ge}_{2}$ and $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$ whose $c$ axis is one-third that of $\zeta_{1}$, since it is difficult to isolate a pure single crystal of $\zeta_{2}$. The analysis is performed on the assumption that the scattering from both crystallites is incoherent. The assumption has been proved to be valid by plotting the diffraction data obtained from a mixed crystal against those from pure $\zeta_{1}$. Full-matrix least-squares refinement has been applied for 384 independent reflections derived from the mixed crystal, which leads to a final $R(F)=$ $0.0885, w R(F)=0.0840$. The composition of $\zeta_{2}{ }^{-}$ $\mathrm{Mn}_{5} \mathrm{Ge}_{2}$ is found to be slightly different from $\zeta_{1}$ by the structure analysis. The atoms in $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$ are located in averaged positions for three parts of the $\zeta_{1}$ structure which are obtained by dividing the structure into three along the $c$ axis.


## Introduction

There are five intermetallic compounds in the $\mathrm{Mn}-\mathrm{Ge}$ system, i.e. $\mathrm{Mn}_{3.25} \mathrm{Ge}, \mathrm{Mn}_{5} \mathrm{Ge}_{2}, \mathrm{Mn}_{2} \mathrm{Ge}, \mathrm{Mn}_{5} \mathrm{Ge}_{3}$ and $\mathrm{Mn}_{11} \mathrm{Ge}_{8}$. The crystal structures of these compounds have been determined and discussed by many authors, for example, Zwicker, Jahn \& Schubert (1949), Kàdàr \& Krèn (1971), Ohba, Ueyama, Kitano \& Komura (1984), Ellner (1980), Castelliz (1953), Israiloff, Völlenkle \& Wittmann (1974) and Ohba, Watanabe \& Komura (1984). Of these, the structure of the high-temperature phase $\zeta-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$, which shows interesting magnetic behavior (Ohoyama, 1961; Wachtel \& Henig, 1969; Yamada, Ohashi \& Ohoyama, 1982; Yamada, Sakai, Usami \& Ohoyama, 1986), is unknown.

An electron microscopic study of the hightemperature phase $\zeta-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$ was made by Kifune \&

[^0]Komura (1986) who found that two types of structures coexist in the alloy specimens and form microsyntactic intergrowth. These two structures have different $c$ values, one is about $39 \AA$ and the other $13 \AA$. We call the former $\zeta_{1}$ and the latter $\zeta_{2}$ in this paper. A mixed crystal of $\zeta_{1}$ and $\zeta_{2}$ shows double peaks in the temperature dependence of magnetization. The crystal structure of $\zeta_{1}-\mathrm{Mn}_{5 \cdot 11} \mathrm{Ge}_{2}$ was determined using a specimen which showed no such double peaks but a single peak in the magnetization (Komura, Ohba, Kifune, Hirayama, Tagai, Yamada \& Ohoyama, 1987).

Intensities of $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$ have been separated from a mixed crystal of $\zeta_{1}$ and $\zeta_{2}$ with the method described in this paper. Intensity data thus derived have been used to determine the crystal structure of $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$, since it is found to be difficult to isolate a pure single crystal of $\zeta_{2}$.

## Experimental

Intensity measurements have been made for three different crystal fragments. One is a single crystal $\zeta_{1}$ of irregular shape, maximum dimension 0.09 mm (sample A), and the other two are mixtures of $\zeta_{1}$ and $\zeta_{2}$, maximum dimensions 0.06 and 0.12 mm (samples $B$ and $B^{\prime}$ ). All the intensity data were collected on a Rigaku automated four-circle diffractometer (AFC5), with graphite-monochromated Mo $K \alpha$ radiation. An $\omega$ scan was employed because of the long $c$ axis of the $\zeta_{1}$ crystal. Experimental conditions for sample $A$ have already been reported (Komura et al., 1987). Conditions for sample $B$ : lattice constants estimated from interplanar spacings are $a=7 \cdot 198(1), c=$ 13.076 (1) and $3 c=39.227$ (4) $\AA$ (mixture) using 25 reflections $\left(19^{\circ}<2 \theta<41^{\circ}\right)$, scan range $(1.5+$ $0.5 \tan \theta)^{\circ}$, scan rate $2^{\circ} \mathrm{min}^{-1}$ in $\theta$, background measurements at the beginning and the end of each scan range for 5 s and the ranges of the data collected were $-9 \leq h \leq 9,-9 \leq k \leq 9,0 \leq l \leq 50$ and $2^{\circ} \leq 2 \theta \leq$ $50^{\circ} ; 1337$ measured reflections with $\left|F_{o}\right| \geq 3 \sigma\left(\left|F_{o}\right|\right)$ averaged to 768 independent reflections. Experimental conditions for sample $B^{\prime}$ are almost the same as those for $B$. Lp and absorption corrections were applied for the samples $A$ and $B$, but not for $B^{\prime}$.

## Analysis of the mixed structure

## A. Comparison of the two kinds of data sets

We have three data sets. One was obtained from a $\zeta_{1}$ single crystal having a simple magnetization curve (Komura et al., 1987) and the other two were obtained from the mixed crystals of $\zeta_{1}$ and $\zeta_{2}$. The data collected from the $\zeta_{1}$ single crystal are called data $A$ and the others from mixed crystals data $B$ and $B^{\prime}$. The data sets $B$ and $B^{\prime}$ did not give good reliability factors when the structure refinements of $\zeta_{1}$ were made (Komura \& Hirayama, 1981). The final $R$ factors obtained were about $10 \%$, and they were not reduced any more. Some atoms have negative temperature factors and some others anomalously large values. As described before, the structure of $\zeta_{1}-\mathrm{Mn}_{5.11} \mathrm{Ge}_{2}$ has been analyzed satisfactorily by using data $A$ (Komura et al., 1987). The structure of the second phase $\zeta_{2}$ has been solved with data $B$ or $B^{\prime}$.

The intensities from samples $A$ and $B$ are represented respectively as follows:

$$
\begin{equation*}
I^{A}(\mathbf{h})=k^{A} I_{39}(\mathbf{h}) \tag{1A}
\end{equation*}
$$

and

$$
\begin{equation*}
I^{B}(\mathbf{h})=k^{B}\left[n_{39} I_{39}(\mathbf{h})+\left(1-n_{39}\right) I_{13}(\mathbf{h})\right], \tag{1B}
\end{equation*}
$$

where $\mathbf{h}$ is a reciprocal-lattice vector, $k^{A}$ and $k^{B}$ are scale factors for samples $A$ and $B$, respectively, $I_{13}(\mathbf{h})$ is the intensity from $\zeta_{2}, I_{39}(\mathbf{h})$ is that from $\zeta_{1}$, and $n_{39}\left(0 \leq n_{39} \leq 1\right)$ is the fraction of $\zeta_{1}$ in sample $B$. We assume here that X-rays are scattered incoherently by $\zeta_{1}$ and $\zeta_{2}$ in the mixed crystal and that structure factors can be calculated by the kinematical diffraction theory. The $c$ axis of $\zeta_{1}$ is exactly three times that of $\zeta_{2}$. The intensity of an $h k l$ reflection having $l=3 n$ in the mixed crystal is considered to be the sum of the intensities from $\zeta_{1}$ and $\zeta_{2}$. On the other hand, $I_{13}(\mathbf{h})$ is equal to zero for reflections with $l \neq 3 n$ $[(1 B)]$. Here the index $l$ is referred to the longer $c$ axis ( $\zeta_{1}$ ). The following relations between $I^{A}(\mathbf{h})$ and $I^{B}(\mathbf{h})$ can be obtained from ( $1 A$ ) and ( $1 B$ ) for $l \neq 3 n$ and $l=3 n$ :

$$
\begin{align*}
I^{A}(\mathbf{h})= & \left(k^{A} / k^{B} n_{39}\right) I^{B}(\mathbf{h}) & & \text { for } l \neq 3 n  \tag{2}\\
I^{A}(\mathbf{h})= & \left(k^{A} / k^{B} n_{39}\right) I^{B}(\mathbf{h}) & & \\
& -\left(k^{A} / n_{39}\right)\left(1-n_{39}\right) I_{13}(\mathbf{h}) & & \text { for } l=3 n .
\end{align*}
$$

Equations (2) and (3) show that $I^{A}(\mathbf{h})$ is proportional to $I^{B}(\mathbf{h})$ for $l \neq 3 n$ reflections, but it is not for $l=3 n$ reflections. $I^{A}(\mathbf{h})$ for $l=3 n$ reflections are smaller than $I^{B}(\mathbf{h})$ multiplied by the scale-factor ratio $k^{A} / k^{B} n_{39}$.

Fig. 1 shows the correlation of intensities between two data sets $A$ and $B$, where the intensities are plotted as $\log |F|$. The symbols $\times$ and $O$ in Fig. 1 represent intensities for $l=3 n$ and $l \neq 3 n$ reflections, respectively. It is clearly shown that $l=3 n$ reflections are distributed lower than $l \neq 3 n$ reflections. Another data
set $B^{\prime}$ was also compared with data $A$, and a similar distribution was obtained. Weaker reflections, which are distributed in the lower left part of the figure, are scattered.

## B. Derivation of the $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$ structure

(i) Intensity of the $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$ structure. Intensity $I_{13}(\mathbf{h})$ for $l=3 n$ can be obtained from (3) by subtracting the intensity $I^{A}(\mathrm{~h})$ from the intensity $I^{B}(\mathrm{~h})$ multiplied by $k^{A} / k^{B} n_{39}$. Although $n_{39}, k^{A}$ and $k^{B}$ are not known, $k^{A} / k^{B} n_{39}$ can be determined by a comparison of reflections with $l \neq 3 n$ [(2)].
A ratio ( $p$ ) of the structure factor of data $A$ to that of $B, p=\left|F_{A}(\mathbf{h})\right| /\left|F_{B}(\mathbf{h})\right|$, which is related to $k^{A} / k^{B} n_{39}$ in (2) and (3), is calculated for every reflection. Averaged values of $p$ are calculated for $l=3 n\left(\bar{p}_{l=3 n}\right)$ and $l \neq 3 n\left(\bar{p}_{l \neq 3 n}\right)$ and are $\bar{p}_{l=3 n}=2.985(5)$ and $\bar{p}_{l \neq 3 n}=5 \cdot 000$ (3) for 411 and 297 reflections, respectively. It is reasonable for $\bar{p}_{l=3 n}$ to be smaller than $\bar{p}_{l \neq 3 n}$ because the intensity of reflection with $l=3 n$ for $B$ comes from both crystals of $\zeta_{1}$ and $\zeta_{2}[(2)$ and (3)]. The value $k^{A} / k^{B} n_{39}$ should be equal to $\bar{p}_{l \neq 3 n}^{2}$ according to (2). The intensity $I_{13}(\mathbf{h})$ is proportional to $\bar{p}_{I \neq 3 n}^{2}\left|F_{B}(\mathbf{h})\right|^{2}-\left|F_{A}(\mathbf{h})\right|^{2}$ according to (3).

For mixed crystals, we have two data sets, $B$ and $B^{\prime}$. If the data for $I_{13}(\mathbf{h})$ derived from both $B$ and $B^{\prime}$ are compared, one can expect a linear relation between them. $199 I_{13}^{\prime}(\mathbf{h}) / I_{13}(\mathbf{h})$ are plotted in Fig. 2, where $I_{13}(\mathbf{h})$ and $I_{13}^{\prime}(\mathbf{h})$ are the intensities derived from $B$ and $B^{\prime}$, respectively. A linear relationship can be observed. Three strong reflections, 030,300 and $1,1,15$, however, deviate from the linear relationship, but these reflections in data set $B^{\prime}$ are affected strongly by extinction owing to the large size of crystal $B^{\prime}$.
The structure of $\zeta_{2}$ can be analyzed using $I_{13}(\mathbf{h})$ derived from the mixed crystal as described above.


Fig. 1. Comparison of two data sets $A$ and $B$. Marks $\times$ and $O$ represent $l=3 n$ and $l \neq 3 n$ reflections, respectively.
(ii) Model of the $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$ structure. The intensity distribution of $I_{13}(\mathrm{~h})$ for the $\zeta_{2}$ structure derived from the mixed crystal is very similar to that for $\zeta_{1}$ with $l=3 n$. Intensity distributions of reciprocal nets 0 kl for $\zeta_{1}$ and $\zeta_{2}$ are shown schematically in Figs. 3(a) and (b), respectively. Patterson maps synthesized from $I_{13}(\mathbf{h})$ are also similar to those of $\zeta_{1}$, so that it may be reasonable to assume that the two crystal structures resemble each other. To obtain an initial model of $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$, the structure of $\zeta_{1}$ (Komura et al., 1987) is divided into three parts along the $c$ axis (Fig. 4a) and the atoms are assumed to be located on the average positions for the three parts (Fig. 4b). There are two kinds of fundamental layers stacked alternately at $c / 30$ in $\zeta_{1}$. Additional atoms are placed on three threefold axes. Atomic positions in the three parts are very similar except for atoms on $00 z$, so that average positions of the atoms on $\frac{12}{3} z, \frac{21}{3} z$ and fundamental layers are easily obtained. Atomic positions on $00 z$ of the three parts of $\zeta_{1}$ are superposed and schematically drawn on a line as shown in Fig. 5. Mn atoms for the initial model of $\zeta_{2}$ were placed between two v marks and Ge atoms were placed between two + marks. Refinements of the $\zeta_{2}$ structure


Fig. 2. Comparison of $I_{13}(\mathbf{h})$ and $I_{13}^{\prime}(\mathbf{h})$ derived from data sets $B$ and $B^{\prime}$, respectively.


Fig. 3. Intensity distributions of the reciprocal nets $0 k l$ for ( $a$ ) $\zeta_{1}$ and $(b) \zeta_{2}$ structures. Index $l$ is referred to the $\zeta_{1}$ structure.
have been carried out using the full-matrix leastsquares method described below.

## C. Refinement of the $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$ structure

The scale factor and positional parameters were refined firstly using 384 independent $I_{13}(\mathbf{h})$ reflections derived from data set $B$, and the $R$ value reached 0.0945 with a fixed temperature factor of $B_{o}=$ $0.8 \AA^{2}$. After refinement with temperature factors, the final $R$ value was $R(F)=0.0885, w R(F)=0.0840$, $w=1, s=1.0937,(\Delta / \sigma)_{\text {max }}=0.07$ and $\Delta \rho$ excursions $\leq|11| \mathrm{e} \AA^{-3}$.* The temperature factors have reasonable values. Determination of the polar direction has not been attempted. The final atomic parameters are listed in Table 1. The program used in the refinement was RADIEL (Coppens, Guru Row, Leung, Stevens, Becker \& Yang, 1979) and scattering factors and anomalous-dispersion corrections $f^{\prime}$ and $f^{\prime \prime}$ for Mn and Ge atoms were taken from International Tables for X-ray Crystallography (1974).

[^1]

Fig. 4. Initial model projected along [010]. Fundamental layers and three threefold axes are represented by horizontal and vertical lines, respectively. Mn and Ge atoms on the threefold axes are represented by open and filled circles, respectively. Kinds of atoms in the fundamental layers are shown by small open and filled circles beside the horizontal lines. (a) $\zeta_{1}$ structure divided into three parts and (b) initial model of $\zeta_{2}$ structure.


Fig. 5. Superposed atomic positions on the 00 z axis of the three parts of $\zeta_{1}-\mathrm{Mn}_{5 \cdot 11} \mathrm{Ge}_{2}$. The $z$ parameter is referred to $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$.

Table 1. Atomic parameters for $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$
$B_{o}$ is an isotropic temperature factor. Designation of atoms is followed in the $\zeta_{1}$ structure.

|  |  | $x$ | $y$ | $z$ | $B_{o}\left(\AA^{2}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Mn}(1)$ | 6(d) | 0.3339 (17) | 0.0295 (15) | ) 0.0 | 0.78 (15) |
| $\mathrm{Mn}(4)$ | 6(d) | 0.6121 (13) | -0.0545 (13) | 0.0945(11) | 0.75 (12) |
| $\mathrm{Ge}(7)$ | 6 (d) | 0.3338 (10) | -0.0065 (13) | 0.1951(11) | 1.11(9) |
| $\mathrm{Mn}(10)$ | 6(d) | 0.6916 (20) | 0.0257 (20) | 0.2963(11) | 1.91 (21) |
| $\mathrm{Mn}(13)$ | 6(d) | 0.3312 (25) | -0.0239 (20) | 0.3900 (6) | 1-10(17) |
| $\mathrm{Mn}(16)$ | $2(a)$ | 0.0 | 0.0 | 0.1201 (14) | 0.97 (25) |
| $\mathrm{Ge}(21)$ | 2(a) | 0.0 | $0 \cdot 0$ | 0.4125 (12) | $1 \cdot 19$ (17) |
| $\mathrm{Ge}(23)$ | 2 (b) | $\frac{1}{3}$ | $\frac{2}{3}$ | -0.0343 (14) | $1 \cdot 38$ (18) |
| Mn (26) | 2 (b) | $\frac{1}{3}$ | ${ }^{\frac{2}{3}}$ | 0.2681 (22) | 1.62 (27) |
| Mn (29) | 2 (c) | ${ }^{\frac{2}{3}}$ | $\frac{1}{3}$ | $0 \cdot 1212$ (15) | 0.75 (25) |
| $\mathrm{Ge}(32)$ | 2(c) | $\frac{2}{3}$ | $\frac{1}{3}$ | 0.4138 (12) | 1.06 (20) |
|  | NO | NV | $R(F) \quad w R(F$ | $w R(F)$ |  |
|  | 384 | 320 | 0.08850 | 0.0840 |  |

Table 2. Interatomic distances $\left(\AA^{2}\right)$ for $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$

| $\mathrm{Mn}(1)-\mathrm{Ge}(32)$ | 2.560 (10) | $\mathrm{Mn}(13)-\mathrm{Ge}(23)$ | $2 \cdot 444$ (18) |
| :---: | :---: | :---: | :---: |
| $\mathrm{Ge}(7)$ | 2.564 (14) | $\mathrm{Ge}(21)$ | $2 \cdot 492$ (20) |
| $\mathrm{Ge}(21)$ | 2.573 (13) | $\mathrm{Ge}(32)$ | 2.516(12) |
| $\mathrm{Ge}(23)$ | $2 \cdot 648$ (13) | $\mathrm{Ge}(7)$ | $2 \cdot 552$ (16) |
| $\mathrm{Mn}(10)$ | $2 \cdot 664$ (14) | $\mathrm{Mn}(10)$ | $2 \cdot 679$ (17) |
| $\mathrm{Mn}(4)$ | $2 \cdot 668$ (17) | $\mathrm{Mn}(4)$ | $2 \cdot 684$ (16) |
| $\mathrm{Mn}(4)$ | 2.672 (13) | $\mathrm{Mn}(10)$ | 2.711 (24) |
| $\mathrm{Mn}(13)$ | 2.758 (24) | $\mathrm{Mn}(10)$ | 2.727 (23) |
| $\mathrm{Mn}(16)$ | 2.789 (15) | $\mathrm{Mn}(26)$ | 2.745 (22) |
| $\mathrm{Mn}(29)$ | 2.792 (13) | Mn (1) | 2.758 (24) |
| Mn (13) | $2 \cdot 827$ (13) | $\mathrm{Mn}(1)$ | $2 \cdot 827$ (13) |
| Mn (13) | $2 \cdot 844$ (25) | $\mathrm{Mn}(1)$ | $2 \cdot 844$ (25) |
| $\mathrm{Mn}(4)$ | $2 \cdot 862$ (16) | $\mathrm{Mn}(16)-3 \mathrm{Ge}(7)$ | 2.617 (12) |
| $\mathrm{Mn}(4)-\mathrm{Ge}(7)$ | $2 \cdot 560$ (16) | 3 Mn (14) | $2 \cdot 639$ (10) |
| Ge (7) | $2 \cdot 564$ (16) | $\mathrm{Ge}(21)$ | 2.715 (24) |
| $\mathrm{Ge}(23)$ | $2 \cdot 620$ (16) | $3 \mathrm{Mn}(1)$ | 2.789 (15) |
| $\mathrm{Mn}(16)$ | $2 \cdot 639$ (10) | $3 \mathrm{Mn}(10)$ | 3-268(20) |
| Mn(29) | $2 \cdot 641$ (10) | $\mathrm{Ge}(21)-3 \mathrm{Mn}(13)$ | 2.492 (20) |
| $\mathrm{Mn}(1)$ | $2 \cdot 668$ (17) | $3 \mathrm{Mn}(1)$ | 2.573 (13) |
| $\mathrm{Mn}(1)$ | $2 \cdot 672$ (13) | $\mathrm{Mn}(16)$ | 2.715 (24) |
| $\mathrm{Mn}(13)$ | $2 \cdot 684$ (16) | $3 \mathrm{Mn}(10)$ | 2.772 (18) |
| $\mathrm{Mn}(10)$ | 2.700 (19) |  | 2.444 (18) |
| $\mathrm{Mn}(1)$ $\mathrm{Mn}(26)$ | $2.862(16)$ $3.029(24)$ | $\mathrm{Ge}(23)-3 \mathrm{Mn}(13)$ $\mathrm{Mn}(26)$ | $2.444(18)$ $2.584(34)$ |
| $\mathrm{Mn}(26)$ $\mathrm{Ge}(7)$ | $3 \cdot 029(24)$ $3 \cdot 130(12)$ | $3 \mathrm{Mn}(4)$ | $2.620(16)$ |
| $\mathrm{Ge}(7)-\mathrm{Mn}(26)$ | $3.130(12)$ $2.537(15)$ | $3 \mathrm{Mn}(1)$ | 2.648 (13) |
| $\mathrm{Ge}(7)-\mathrm{Mn}(26)$ $\mathrm{Mn}(13)$ | $2.537(15)$ $2.552(16)$ | $\mathrm{Mn}(26)-3 \mathrm{Ge}(7)$ | $2.537(15)$ |
| $\mathrm{Mn}(1)$ | $2.564(14)$ 2.564 | $\mathrm{Ge}(23)$ | 2.584 (34) |
| $\mathbf{M n}(4)$ | 2.560 (16) | $3 \mathrm{Mn}(10)$ | 2.608 (11) |
| $\mathrm{Mn}(4)$ | 2.564 (16) | $3 \mathrm{Mn}(13)$ $3 \mathrm{Mn}(4)$ | 2.745 (22) |
| Mn(29) | 2.607 (11) | 3Mn(4) | $3 \cdot 029$ (24) |
| Mn(16) | 2.617(12) | Mn (29)-3Ge(7) | $2 \cdot 607(11)$ |
| $\mathbf{M n}(10)$ | 2.624 (20) | $3 \mathrm{Mn}(4)$ | 2.641 (10) |
| $\mathbf{M n}(10)$ | $2 \cdot 800$ (18) | $\mathrm{Ge}(32)$ | $2 \cdot 712$ (25) |
| $\mathrm{Mn}(10)$ | 2.812(15) | 3 Mn (1) | 2.792 (13) |
| $\mathrm{Mn}(4)$ | 3.130 (12) | $3 \mathrm{Mn}(10)$ | 3.251 (20) |
| $\mathrm{Mn}(10)-\mathrm{Mn}(26)$ | $2 \cdot 608$ (11) | $\mathrm{Ge}(32)-3 \mathrm{Mn}(13)$ | 2.516 (12) |
| $\mathrm{Ge}(7)$ | $2 \cdot 624$ (20) | $3 \mathrm{Mn}(1)$ | $2 \cdot 560$ (10) |
| $\mathrm{Mn}(1)$ | 2.664 (14) | $\mathrm{Mn}(29)$ | 2.712 (25) |
| $\mathrm{Mn}(13)$ | 2.679 (17) | $3 \mathrm{Mn}(10)$ | 2.774 (18) |
| $\mathrm{Mn}(4)$ | 2.700 (19) |  |  |
| $\mathrm{Mn}(13)$ | 2.711 (24) |  |  |
| Mn(13) | $2 \cdot 727$ (23) |  |  |
| $\mathrm{Ge}(21)$ | 2.772 (18) |  |  |
| $\mathrm{Ge}(32)$ | 2.774 (18) |  |  |
| $\mathrm{Ge}(7)$ | $2 \cdot 800$ (18) |  |  |
| $\mathrm{Ge}(7)$ | $2 \cdot 812$ (15) |  |  |
| Mn(29) | $3 \cdot 251$ (20) |  |  |
| $\mathrm{Mn}(16)$ | $3 \cdot 268$ (20) |  |  |

The refinement was also made using intensities $I_{13}(\mathbf{h})$ derived from data set $B^{\prime}$. The positional parameters obtained are the same as those of $B$ within $3 \sigma$. Since we reach the same results for the structure from the different data sets, it is concluded that the structure of $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$ is determined correctly.

## Discussion

The structure of $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$, whose $c$ axis is one-third of $\zeta_{1}-\mathrm{Mn}_{5.11} \mathrm{Ge}_{2}$, has been determined using the intensities derived from a mixed crystal. As described above, we already know the structure of $\zeta_{1}-\mathrm{Mn}_{5.11} \mathrm{Ge}_{2}$ (Komura et al., 1987). If the calculated intensity data $I_{39}(\mathbf{h})$ from the $\zeta_{1}$ structure are substituted in (1B), with $k^{B} n_{39}$ known from (2) for $l \neq 3 n$, the intensity data $I_{13}(\mathbf{h})$ can be obtained independently from the above method. The structure refinement has been carried out using this data set and the positional parameters thus obtained lead to the same values within errors of $3 \sigma$. We utilized one data set from a pure single crystal in this paper. However, this method can be applied even without having single-crystal data if one has two data sets of mixed crystals of different compositions.

The composition of $\zeta_{2}$ is slightly different from $\zeta_{1}$ according to the refinement; the number of Mn atoms on $00 z$ is two for $\zeta_{2}$ and eight for $\zeta_{1}$ even though the $c$ axis is three times longer than that of $\zeta_{2}$ (Fig. 5). $\zeta_{2}$ is then described exactly by $\mathrm{Mn}_{5} \mathrm{Ge}_{2}$, and $\zeta_{1}$ by $\mathrm{Mn}_{5 \cdot 11} \mathrm{Ge}_{2}$. The difference between them is small, and it is practically impossible to distinguish them by chemical analysis since both crystallites make microsyntactic intergrowth.

Interatomic distances for $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$ are listed in Table 2. The coordination number of Mn atoms in $\zeta_{2}$ is 12 or 13 and that of Ge atoms 10 or 11 , which is similar to the $\zeta_{1}$ structure.

The crystallites of $\zeta_{2}$ make microsyntactic intergrowth with $\zeta_{1}$ as was observed under the electron microscope (Kifune \& Komura, 1986). The width of the bands of intergrowth is about $1000 \AA$. Although an effort to find a single crystal of $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$ was made, no such crystal was obtained even under the electron microscope. The validity of the treatment of the incoherent-scattering calculation from both crystallites is apparent in Fig. 1. If coherent scattering is dominant, cross terms of $F$ and $F^{*}$ appear in (1B). In general, cross terms of $F$ and $F^{*}$ cannot be known as positive or negative. So $l=3 n$ reflections are distributed randomly above and below $l \neq 3 n$ reflections. Weaker reflections, which are distributed in the lower left part in Fig. 1, are seen to form two groups. Attempts to find the reason have not yet succeeded.
It is remarkable that the difference in the structure may reflect sensitively on the magnetic properties. It is necessary to obtain a single domain of $\zeta_{2}$ in order
to find the detailed relationship between the structure and the magnetic properties.

The calculations were carried out on a HITAC $\mathrm{M}-200 \mathrm{H}$ computer at the Information Processing Center of Hiroshima University and a personal computer, Fujitsu FM-11EX, in our laboratory.

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[^1]:    *A list of structure factors for $\zeta_{2}-\mathrm{Mn}_{5} \mathrm{Ge}_{2}$ has been deposited with the British Library Document Supply Centre as Supplementary Publication No. SUP 44108 ( 4 pp .). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.

